



33 features into modular robot designs significantly enhances their adaptability and  
34 multifunctionality in aquatic environments.

35 **Keywords:** Modular Robot, Soft Robot, Manipulation, Locomotion, Structure  
36 Formation

37 When we think about modular robots, we think the robots can combine together to do  
38 more complex tasks. Soft robots offer significant potential for complex, dynamic envi-  
39 ronments due to their compliance and mechanical intelligence, especially in aquatic  
40 scenarios where they can adapt to water flow and handle fragile objects. Their  
41 application in aquatic domains remains largely unexplored. To address this gap, we  
42 present SoftRafts, a robotic platform that seamlessly integrates softness and mod-  
43 ularity for on-water operations. Our design combines rigid 3D-printed components  
44 with soft foam, featuring a cable-actuated mechanism and propeller for unteth-  
45 ered aquatic locomotion. The robot modules can not only connect to form complex  
46 structures for collaborative tasks (Fig. 1(i)) but also switch between soft and rigid  
47 modes, enabling unprecedented versatility. The demonstrated capabilities of SoftRafts  
48 span from amphibious navigation and diverse object manipulation to constructing  
49 deformable, variable-stiffness lattices, showcasing the unique advantages of combining  
50 soft robotics with modular design in aquatic environments.

51 In nature, many species, such as ants and dolphins work collectively to solve  
52 challenges related to locomotion, manipulation, or structure assembly [1–4]. For  
53 example, beavers collaborate to construct dams and lodges [1], while ants work col-  
54 lectively to move heavy and large objects and build rafts from their bodies to survive  
55 floods [2, 3, 5]. Inspired by such natural swarm systems, robot swarms emulate col-  
56 lective behavior to tackle complex tasks beyond the capability of a single robot.  
57 Modular robotics builds on this concept by enabling individual units to assemble into  
58 larger lattices, forming robots in various configurations to accomplish diverse tasks [6–  
59 8]. Significant progress has been made in terrestrial modular robots [9–11], such as  
60 SMORES [11, 12] and Sambot [13]. Recently, researchers have extended these con-  
61 cepts to outdoor environments, transitioning locomotion and manipulation tasks from  
62 indoor settings. Examples include snail-inspired robots [14] and multi-legged robot  
63 swarms [15].

64 However, research on modular robots designed for aquatic applications remains  
65 limited [8]. The majority of current aquatic reconfigurable modular robots are designed  
66 as waterborne vehicles or boats [8], excelling at tasks such as forming rigid floating  
67 platforms or enabling precise maneuverability. One notable example is a study from  
68 Yim’s group in 2015 [16], which introduced the first aquatic modular reconfigurable  
69 robots. This work developed a swarm of boats, each equipped with four propellers  
70 for precise maneuverability, capable of autonomously connecting side-by-side to form  
71 larger, lattice-like structures. Another example comes from Rus’ group at MIT [17],  
72 where a fleet of autonomous boats was designed to disconnect and reassemble into var-  
73 ious configurations. These boats demonstrated the ability to form floating structures,  
74 such as rearranging three robots from a connected straight line into an “L” shape.

75 To expand their capabilities, incorporating soft materials into modular robot  
76 designs introduces a new dimension of adaptability and versatility. Soft materials pro-  
77 vide compliance [18], enabling robots to conform to uneven surfaces, interact more  
78 effectively with fragile or irregular objects, and provide mechanical intelligence, which  
79 allows them to passively adapt to external stimuli, such as bending under pressure or  
80 flexing to reduce drag, thereby enhancing their ability to perform complex tasks in dif-  
81 ferent aquatic environments [19]. When integrated with variable stiffness mechanisms,  
82 soft modular robots can transit between compliant states for flexibility and stiffened  
83 configurations for load-bearing or structural tasks. This dual capability enhances the  
84 functionality of existing designs, enabling new applications such as diverse manipula-  
85 tion tasks and merging multiple functionalities into a single platform. These robots can  
86 form adaptable floating platforms, construct deformable lattices for various manipu-  
87 lation tasks, perform different types of locomotion, and transform into various shapes  
88 to meet the demands of complex scenarios.

89 Designing waterproof, untethered, aquatic soft modular robots presents significant  
90 challenges due to the interplay of various factors that must be carefully addressed.

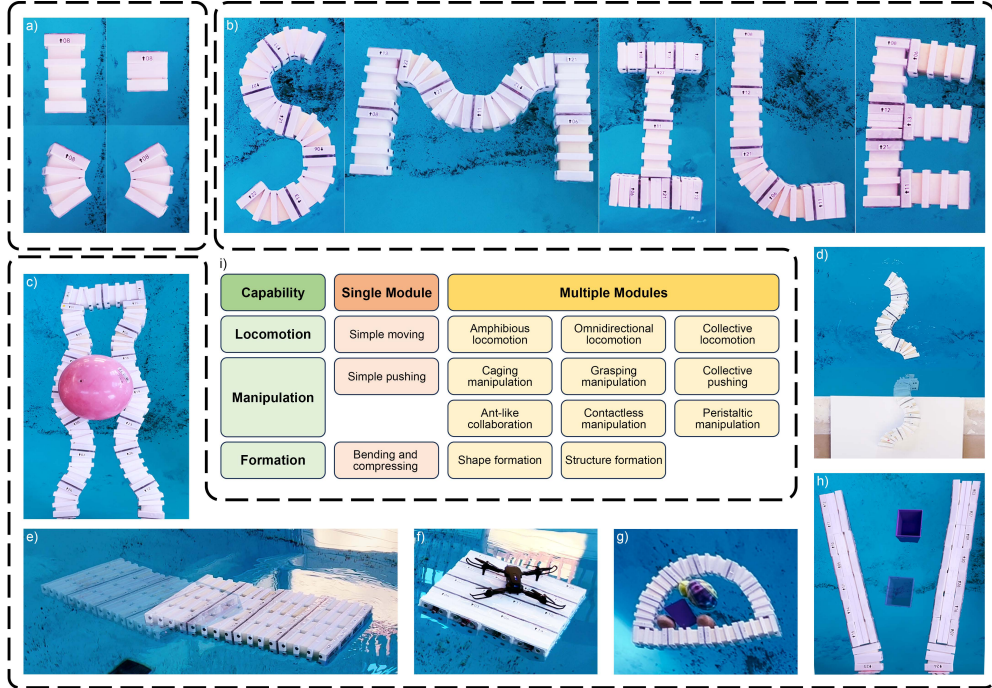
91 i) Actuation is one of the primary considerations. Different actuation methods  
92 for soft robots, such as thermal-responsive systems [9], cable-driven mechanisms [20],  
93 pneumatics [21], electrically-responsive methods [22, 23], and magnetically-responsive  
94 approaches [24], among others, offer distinct advantages and trade-offs. Enabling  
95 untethered operations while achieving essential functionalities—such as bending, steer-  
96 ing, locomotion, and variable stiffness—poses a significant challenge in selecting the  
97 appropriate actuation method. The chosen method must balance precision, efficiency,  
98 and compactness to meet the demands of an untethered aquatic modular system.

99 ii) Material selection is equally crucial, as the materials must provide both softness  
100 for compliance and flexibility, as well as the ability to transition to a rigid state for  
101 load-bearing or structural tasks. Commonly used materials in soft robotics include  
102 silicone, foam, and other elastomers [25, 26], which offer a good balance between  
103 deformability and durability. However, for building multiple modules—particularly  
104 when scaling up to more than 20—the fabrication process becomes a significant factor.  
105 It must be efficient, consistent, and scalable to ensure uniformity and functionality  
106 across all modules while maintaining the desired material properties. Addressing these  
107 fabrication challenges is essential to achieve reliable performance in complex, large-  
108 scale robotic assemblies.

109 iii) Waterproofing and untethering present critical challenges [27, 28], particu-  
110 larly in cable-driven systems where delicate internal mechanisms must be safeguarded  
111 against water ingress. The direct exposure of cables to water necessitates the isola-  
112 tion of the winch and motor while simultaneously maintaining dynamic waterproofing  
113 to allow continuous operation. The design must ensure that actuators, cables, and  
114 electronic components remain securely sealed, providing robust protection without  
115 compromising the system’s motion or overall functionality.

116 iv) Interconnection methods between modules are also a key challenge. The con-  
117 nections must enable robust attachment while ensuring the seamless transmission of  
118 forces and motion between modules [29]. This is particularly important for creating

119 adaptable, reconfigurable systems that can form larger structures or perform collabora-  
 120 tive tasks. The placement and design of connectors significantly influence the assembly  
 121 patterns and the versatility of the system [19]. For example, to achieve all-directional  
 122 connectivity, as demonstrated in StarBlocks [10], the connectors must be strategically  
 123 positioned to allow for flexible reconfiguration, ensuring compatibility with a wide  
 124 range of assembly geometries and operational demands.



**Fig. 1 Overview of the capability of SoftRaft modular robot in a single module and multiple modules.** (a) Single module shape deformation. (b) Robots form ‘SMILE’ shapes and structures. (c) Two chains of modules manipulate a ball using peristaltic manipulation. (d) A chain of modules locomotes from the ground and gets in the water. (e) A raft combined with multiple modules that can move in the water. (f) Multiple modules formed a rigid raft structure that allows a drone to land on it. (g) Caging manipulation. (h) Water flow contact-less manipulation. (i) Capability table between a single module and multiple modules comparison.

125 In this work, we aim to advance the development of untethered, aquatic soft modu-  
 126 lar robots capable of reliable operation in dynamic environments. By enabling softness  
 127 through aquatic modular robots, we address this critical gap and demonstrate the  
 128 concept’s potential through various application scenarios. To address the identified  
 129 design challenges, we drew inspiration from the principles of push puppets to develop  
 130 a cable-driven system with two strings. Each module combines 3D-printed rigid compo-  
 131 nents with soft foam components and incorporates a propeller for rapid locomotion  
 132 on water. By shortening strings, the robot can deform into the curve or transit from

133 a soft, compliant state to a fully rigid state, enabling a seamless switch between tasks  
134 that require flexibility or structural rigidity. To achieve waterproofing and untethered  
135 operation, we implemented wireless charging and developed a mechanism to isolate  
136 the winch from the motor to ensure reliable performance in submerged conditions.

137 We evaluated the robot’s capabilities across three core functionalities: locomotion,  
138 manipulation, and formation (Fig. 1(i)). For locomotion, individual modules perform  
139 simple motions, while multi-module configurations, such as chains for amphibious  
140 movement on ground and water (Fig. 1(d)) and plus-sign structures for omnidirectional  
141 navigation (Fig. 7(b)), showcase versatility. Manipulation tasks leverage configura-  
142 tions like caging for transporting objects (Fig. 1(g)), contactless manipulation through  
143 water currents (Fig. 1(h)), and wave-phase strategies for non-prehensile operations  
144 (Fig. 1(c)). It also able to manipulate object collectively (Fig. 5(c,d)). For formation,  
145 individual modules perform simple motions (Fig. 1(a)), while multi-module configu-  
146 rations, such as (Fig. 1(b)) present the shape formation and structure formation to  
147 show the word ‘SMILE’. The robots assemble into rafts for drone landing platforms  
148 (Fig. 1(f)) (Fig. 4(c)), bridges for moving small vehicles (Fig. 4(d)), or carriers sup-  
149 porting multiple decks for aircraft operations (Fig. 4(e)). These experimental results  
150 demonstrate the versatility of the design and its enhanced capabilities when multi-  
151 ple modules are combined, underlining the potential of this approach for addressing  
152 diverse tasks in complex aquatic environments.

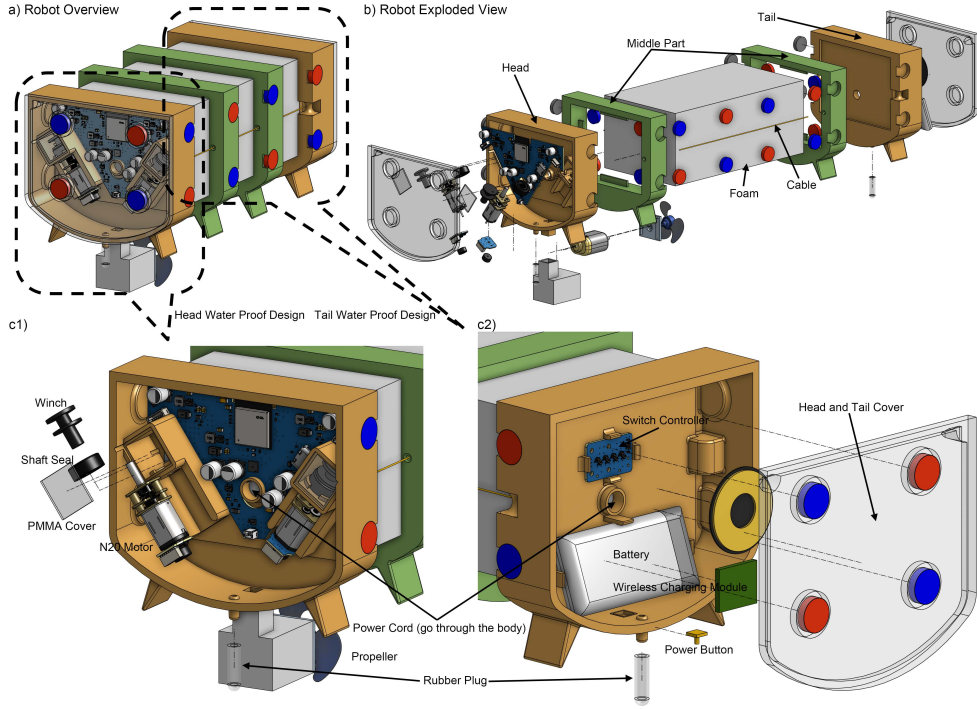
## 153 Results

### 154 Mechanism overview

155 Each robot in the modular system is composed of four rigid components and a soft foam  
156 core, as depicted in Fig. 2. The front and rear rigid components (Head and Tail) house  
157 the controller (printed circuit board–PCB), power supply (battery), and actuators  
158 (motors). The two middle rigid components form a structural frame that securely  
159 holds the foam core, which is chosen for its buoyant and flexible properties. This design  
160 allows the foam to compress fully within the middle rigid frames, facilitating seamless  
161 transitions between soft and rigid states while maintaining a compact structure.

162 The robot features three primary controllers: two motors, located within the rigid  
163 head container, which control the left and right strings to enable precise bending  
164 movements. A third motor, housed in a 3D-printed component for protection attached  
165 to the rigid head part, drives a propeller for forward and backward motion. The rear  
166 rigid container houses a sealed battery, a wireless charging module, a switch controller  
167 for power, and a power button for operation. The power cord runs from the rear  
168 components to the head components, passing through the middle of the soft foam,  
169 as depicted in Fig. 2(c1,c2). This separation design balances the mass and buoyancy  
170 along the robot.

171 Waterproofing the cable-driven system was accomplished by isolating the winch  
172 from the motors using a combination of a shaft seal, waterproof grease, and an acrylic  
173 (PMMA) cover, as illustrated in Fig. 2(c1). To ensure each robot is waterproof, two  
174 rubber plugs are used: one at the bottom of the rigid part of the head and the other at  
175 the tail part. Once all parts are sealed, the waterproofing is tested in two stages: static

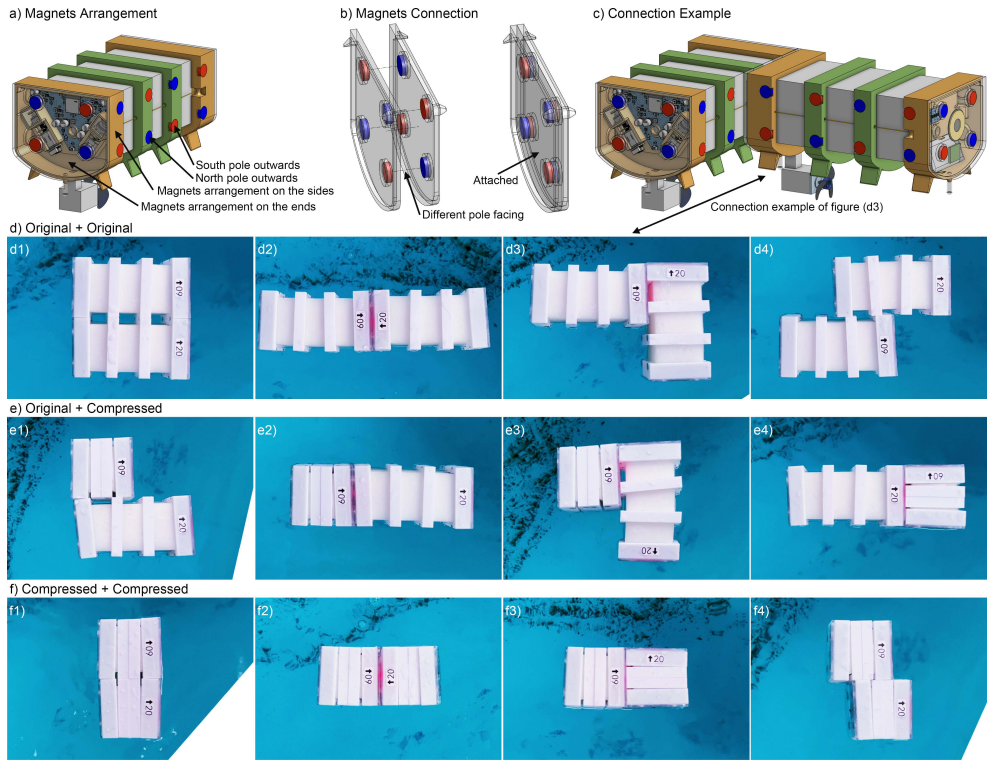


**Fig. 2 Mechanism overview of a single robot.** Head and Tail parts are 3D printed with resin, while the Middle parts are 3D printed with PETG. **(a)** CAD model of a complete single module. **(b)** Exploded view of a single module. **(c1)** Head part water proof design dissection, **(c2)** Tail part water proof design dissection.

176 and dynamic tests. In the static test, air is injected into both containers using a syringe,  
 177 and the system observed approximately full rebound in the syringe, indicating a sealed  
 178 environment. If the static test is successful, the robot is submerged in water and tested  
 179 if any bubbles appear when pushing the air into the chamber. For the dynamic test, the  
 180 propellers and motors are activated while the robot operates underwater to confirm  
 181 the waterproofing under real-world conditions.

182 The configuration space of a single robot is determined by the lengths of two  
 183 strings,  $s_1$  and  $s_2$ , which control its deformation. The original width-to-length ratio  
 184 of the robot is 1:2. The purpose of this design is can achieve symmetric attachment  
 185 in both the original and compressed state. When both strings are shortened to half  
 186 their original length, the robot transitions from a soft to a rigid state, allowing it to  
 187 sustain a maximum load of 0.4 kg. If only one string is shortened, the robot bends to  
 188 one side, enabling shape formation and steering. As illustrated in Fig. 1(a), the robot  
 189 can achieve four primary states: the original state ( $s_1 = s_2 = s$ ), bending to the left  
 190 ( $s_1 = \frac{1}{2}s, s_2 = s$ ), bending to the right ( $s_1 = s, s_2 = \frac{1}{2}s$ ), and the compressed state  
 191 ( $s_1 = s_2 = \frac{1}{2}s$ ). Since the string lengths can vary continuously, the robot can achieve  
 192 an infinite number of intermediate states, resulting in a highly versatile configuration  
 193 space.

194 Beyond its deformation capabilities, the robot can perform locomotion and simple  
 195 manipulation tasks using its propeller. A single robot's Cost of Transport (CoT) is  
 196 approximately 68.35, calculated using the equation  $\text{CoT} = \text{Power}/(\text{Weight} \cdot \text{Speed})$ ,  
 197 where  $\text{Power} = 8.66 \text{ W}$  represents the average energy consumption,  $\text{Weight} = 0.384 \text{ kg}$   
 198 is the mass of the robot, and  $\text{Speed} = 0.33 \text{ m/s}$  is the robot's maximum velocity  
 199 when moving forward in calm water conditions. We also designed six different motion  
 200 primitives and tested how each primitive affected the robot's position and orientation  
 201 to understand its locomotion capabilities. The six gaits include *forward*, *backward*,  
 202 *left\_front*, *right\_front*, *left\_back*, and *right\_back*. Figure S1 shows the global  $x$ - $y$  positions  
 203 achieved by the robot under each gait, assuming an initial position and orientation  
 204 of  $(0, 0, 0)$ . The cluster centers for each gait are marked with stars (\*), with dashed  
 205 lines indicating the robot body orientation based on the average  $\theta$  of the gait. The  
 206 origin  $(0, 0)$  represents the robot's starting position, with a dashed black line showing  
 207 its initial orientation parallel to the  $x$ -axis.



**Fig. 3 Magnet arrangement and connection configurations between two modules.** (a) Magnet arrangement on a single robot. (b) Magnet-based connection mechanism. (c) Example of a connection between two modules. (d) Four possible connection configurations when both modules are in their original state. (e) Four connection configurations when one module is in the original state and the other is compressed. (f) Four connection configurations when both modules are compressed.

208 **Connectivity**

209 In terms of connectivity, each robot is equipped with magnetic connectors on all  
210 four sides—front, back, left, and right—enabling versatile multi-robot configurations.  
211 The detailed magnet arrangement is shown in Fig. 3(a,b,c), which supports connec-  
212 tions between robots from various directions (Fig. 3(d)). When compressed, the robot  
213 forms a square from a top-down view, facilitating attachments in multiple orientations  
214 (Fig. 3(e,f)). This design allows the robots to assemble into various shapes tailored for  
215 specific tasks. For example, they can form snake-like chains for locomotion on both  
216 ground and water (Fig. 7(a)), a plus-sign shape with five modules for omnidirectional  
217 locomotion (Fig. 7(b)), or larger lattice structures for manipulation and the construc-  
218 tion of movable platforms (Fig. 4(d)). The magnetic connectors exhibit significant  
219 strength, supporting approximately 2 kg before detachment, ensuring stability and  
220 reliability in multi-robot assemblies.

221 **Shape and structure formation**



**Fig. 4 Structure formation and shape formation of multiple modules. (a)** A chain of modules forms an ‘S’ shape. **(b)** Three chains of modules form an ‘I’ structure. **(c)** Multiple modules form a soft raft and then compress into a rigid raft, which allows a drone to land on it. **(d)** A lot of modules form a bridge, allowing a toy car to run on it. **(e)** Multiple modules form two platforms with a flat board on it. Perform as an aircraft carrier.



222 **Shape formation**

223 Our modular robots can form various shapes and structures by deforming mod-  
 224 ules or through different assembly configurations (shown in Movie S1). As shown in  
 225 Fig. 4(a,b), examples include forming letters such as “I” and “E” through specific  
 226 arrangements and assembly methods. For a chain of robots, shapes like the letters “S”  
 227 and “L” can be achieved by adjusting the string lengths of each module. The letter  
 228 “M” combines both approaches: three chains are first assembled into a door-like shape,  
 229 after which the middle chain deforms to complete the “M” shape. This versatility  
 230 highlights the modular robots’ adaptability in forming complex structures.

231 For a chain of modules to deform into different shapes, an analytical relationship  
 232 exists between the string lengths  $s_1$ ,  $s_2$ , the angle  $\theta$ , and the length  $L$  of the middle  
 233 curve of the robotic structure. The structure comprises four rigid 3D-printed compo-  
 234 nents, denoted as  $r_1$ ,  $r_2$ ,  $r_3$ , and  $r_4$ , each with a length  $l_r$ . Figure S2 illustrates the  
 235 geometric configuration of the structure.

236 In the forward kinematics process, the resulting shape of the robot chain is  
 237 calculated based on the given string lengths  $s_1$  and  $s_2$ . The equations are as follows:

238 For  $s_1 \leq s_2$ :

$$\theta = 3 \cos^{-1} \left( 1 - \frac{(s_2 - s_1)^2}{18l_r^2} \right), \quad L = \frac{s_1 + s_2}{2}.$$

239 For  $s_1 > s_2$ , the angle becomes negative:

$$\theta = -3 \cos^{-1} \left( 1 - \frac{(s_2 - s_1)^2}{18l_r^2} \right), \quad L = \frac{s_1 + s_2}{2}.$$

240 At the initial state ( $s_1 = s_2 = L$ ), the robot remains undeformed ( $\theta = 0$ ).

241 In the inverse kinematics process, the required string lengths  $s_1$  and  $s_2$  are deter-  
 242 mined to achieve a desired curve characterized by specific values of  $L$  and  $\theta$ . The  
 243 equations are:

$$s_1 = L - \frac{1}{2}\Delta s, \quad s_2 = L + \frac{1}{2}\Delta s,$$

244 where

$$\Delta s = \sqrt{18l_r^2 \left( 1 - \cos \left( \frac{\theta}{3} \right) \right)}.$$

245 If  $\theta < 0$ , the values of  $s_1$  and  $s_2$  are swapped to reflect the negative angle.

246 These equations establish the relationship between the string lengths, the angle  
 247  $\theta$ , and the middle curve length  $L$ , enabling precise control of the robot’s shape. This  
 248 analytical framework allows the chain of robots to adopt a wide range of shapes tailored  
 249 to meet the demands of diverse tasks. The derivation of these equations is detailed in  
 250 the supplementary methods under “Kinematics of Modular Robot”.

## 251 **Structure formation**

252 Our robots demonstrated their versatility by forming various lattice structures for dif-  
253 ferent applications (shown in Fig. 4 and Movie S1). In one example, the robots were  
254 configured into a flat lattice structure to serve as a temporary, movable platform for  
255 drone landing, as shown in Fig. 4(c). This lattice could move omnidirectionally and  
256 compress into a rigid platform, providing a stable and adaptable surface for drone  
257 operations. In another example, the robots were assembled into a larger lattice struc-  
258 ture to form a bridge capable of supporting the movement of a small toy car, showing  
259 the robots' ability to create structures for potential transportation tasks (Fig. 4(d)).  
260 Additionally, two separate movable platforms, each constructed with modular robots  
261 and topped with a rigid board, were joined together to simulate an aircraft carrier.  
262 This assembly, illustrated in Fig. 4(e), demonstrated the potential of scalability and  
263 adaptability of the modular robots for larger, more complex structures.

264 We have tested the maximum load of the robot in the rigid mode, which is designed  
265 to sustain weight. The load for a single module is about 400 g. The load can be a  
266 linear superposition with more modules.

## 267 **Manipulation**

268 Our robots are capable of various manipulation strategies to interact with and move  
269 objects. This section explores four key manipulation techniques: caging, grasping,  
270 non-prehensile manipulation, and contactless manipulation.

### 271 **Caging: trash collection, transport, and enclosure**

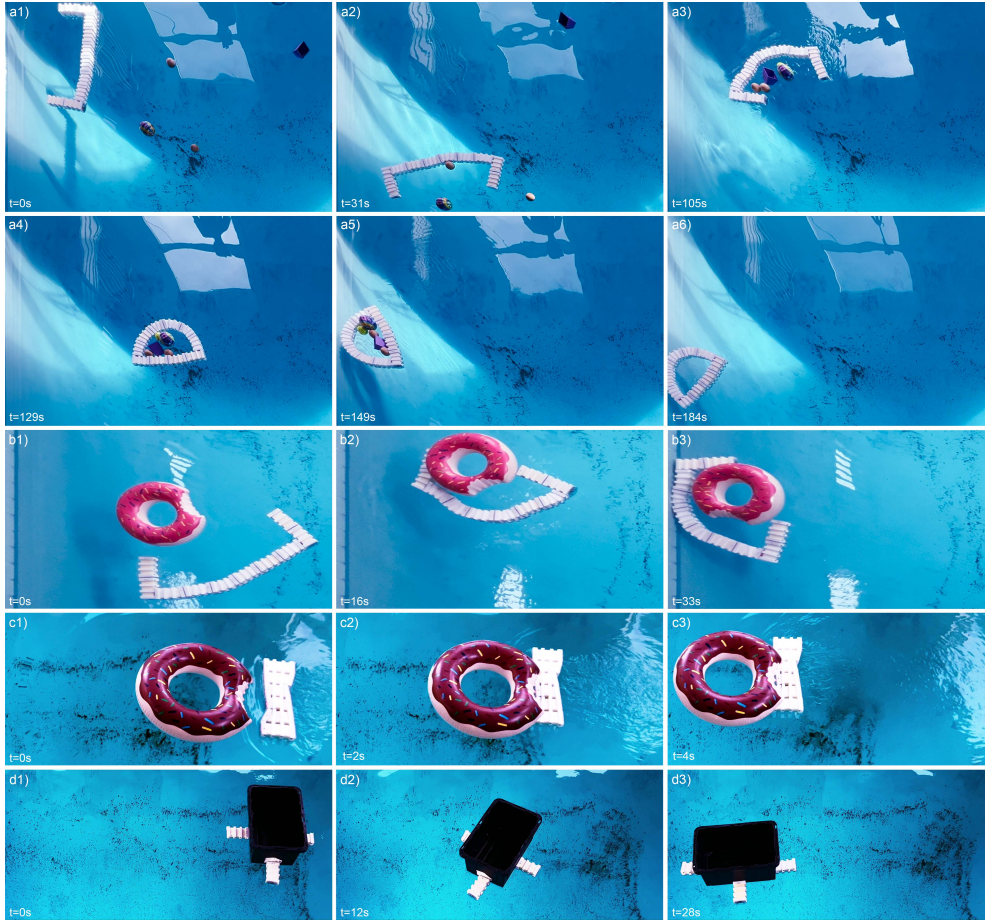
272 Our modular robots can form structures to surround and manipulate objects, enabling  
273 tasks such as trash collection, transport, and water enclosure. Caging stabilizes objects  
274 by forming a complete or partial enclosure. Once enclosed, the robots coordinate their  
275 movements to transport the object while maintaining the enclosure.

276 One example is a gripper-like caging configuration (shown in Fig. 5(a) and Movie  
277 S1), where three chains of modules are connected into a door shape. The left and right  
278 chains are used for steering and moving the structure. Control primitives allow the  
279 gripper to move forward, left, and right, enabling real-time operation for collecting and  
280 transporting trash. After the objects are collected, a fully enclosed caging mechanism  
281 ensures that all objects remain securely contained during transport.

282 This strategy is particularly effective for transporting irregularly shaped, fragile, or  
283 small objects that require a stable hold without direct physical contact. By maintaining  
284 the object within a stable formation, the caging approach ensures safe and efficient  
285 transport across dynamic aquatic environments.

### 286 **Grasping for secure object transport**

287 In the grasping strategy, the robots form a full loop around the object and contract  
288 inward to securely grip it. Unlike caging, grasping involves a tighter hold for greater  
289 control. Once grasped, the robots coordinate their movements to transport the object  
290 while maintaining a secure grip. (Fig. 5(b) and Movie S1) shows an example of a 2D  
291 gripper grasping a swim ring.



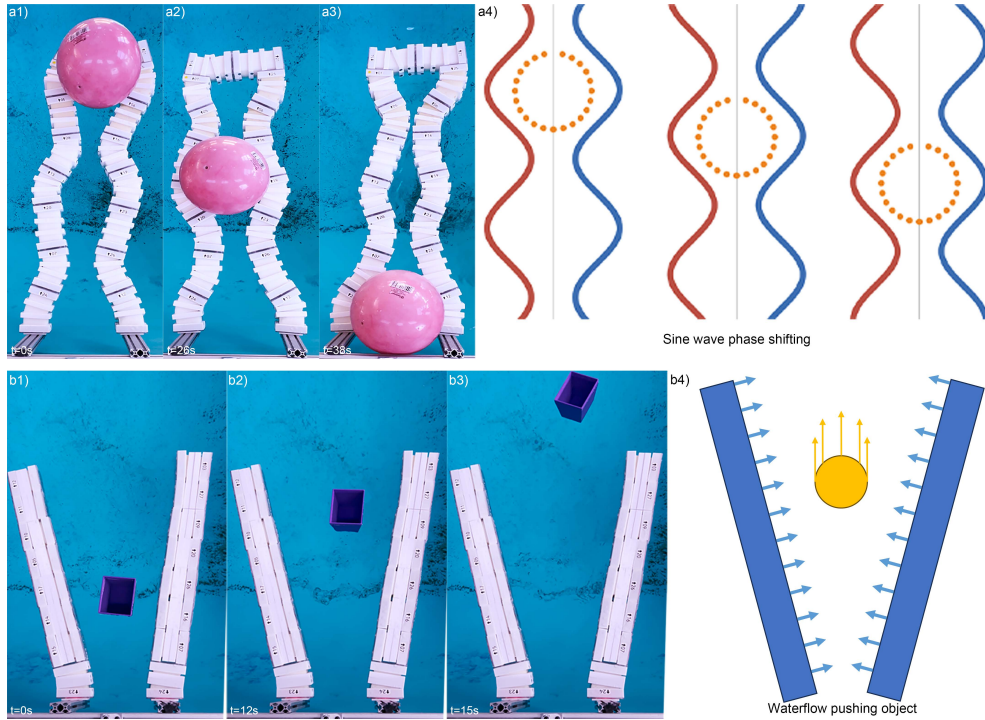
**Fig. 5 Manipulation of multiple modules.** (a) Caging manipulation. A robot cage formed with multiple blocks moving on the water, collecting objects floating on it, and then caging them securely. (b) Grasping manipulating. For large objects, the robot cage can act as a gripper and grasp the object to manipulate. (c) Pushing manipulation. A pile of modules deforms into the matching shape and pushes the object floating on the water. (d) Ant-like collaborative omnidirectional manipulation. For blocks to push the object together, by controlling the pushing force, the object can move in any direction.

## 292 Non-prehensile manipulation

293 Non-prehensile manipulation involves interacting with objects without fully enclosing  
 294 or grasping them. Instead, this approach relies on external forces or coordinated con-  
 295 figurations to achieve desired tasks. Our modular robotic system demonstrates two  
 296 distinct non-prehensile manipulation strategies:

297 **Multi-robot collaboration for moving large objects.** Inspired by the behav-  
 298 ior of ants moving large objects [3], multiple robots coordinate to apply synchronized  
 299 forces to manipulate objects with physical contact but without physically attaching to

300 them. This strategy enables the robots to collectively push or pull large objects, such  
 301 as boxes or swim rings, by leveraging distributed force application. Fig. 5(d) and Movie  
 302 S1 illustrates an example where four modules work collaboratively to push a box in  
 303 different directions. To maintain contact with the box without physically attaching to  
 304 it, the propellers of all modules are carefully controlled. For instance, if robots *A*, *B*,  
 305 *C*, and *D* are arranged clockwise, moving the box toward robot *A* requires the pro-  
 306 pellers of robots *A*, *B*, and *D* to operate at low speed to maintain contact, while robot  
 307 *C* increases its propeller speed to generate the required net force toward robot *A*.  
 308 Another example, shown in Fig. 5(c) and Movie S1, involves a chain of modules con-  
 309 nected side-by-side to push a swim ring. The modules deform to better fit the shape  
 310 of the swim ring, and propeller control is used to steer and move the entire chain.



**Fig. 6 Manipulation with two chains of robots. (a)** Wave phase changing non-prehensile manipulation. The robot squirms with the Sine wave pattern to manipulate the ball. **(b)** Water flow contactless manipulation. The robot uses propellers to create water flow, which can manipulate objects.

311 **Peristaltic manipulation.** This method uses two parallel chains of robots to gen-  
 312 erate wave-like contractions for moving objects. The motion is achieved by sequentially  
 313 tightening and relaxing the string lengths of each module, producing a wave-like defor-  
 314 mation similar to biological peristalsis. To implement this, one chain of robots is fitted  
 315 to a sinusoidal curve, described mathematically as  $y = \sin(x + t)$ , where  $t$  represents

316 a phase shift over time. The second chain mirrors this curve symmetrically across the  
317 middle axis. The sinusoidal motion is discretized into six distinct stages per period,  
318 corresponding to evenly spaced phase shifts of  $\frac{\pi}{3}$  radians ( $60^\circ$ ). Each stage determines  
319 the desired string lengths  $s_1$  and  $s_2$  for each robot in the chain. These lengths are com-  
320 puted based on the required deformation to match the sinusoidal shape, as derived  
321 from the inverse kinematics equations. By iterating through these stages, the chains  
322 generate a traveling wave that applies periodic pressure to objects positioned between  
323 them, propelling the object forward.

324 The sequence of six stages ensures a continuous wave motion, with each robot  
325 transitioning smoothly between states to maintain a stable and consistent force on  
326 the object. This method is particularly effective for manipulating objects through  
327 narrow spaces or over uneven surfaces, as the wave motion dynamically adjusts to  
328 accommodate irregularities. Fig. 6(a) and Movie S1 illustrates the stages of the wave-  
329 like motion and the corresponding deformation of the robot chains.

### 330 **Contactless manipulation**

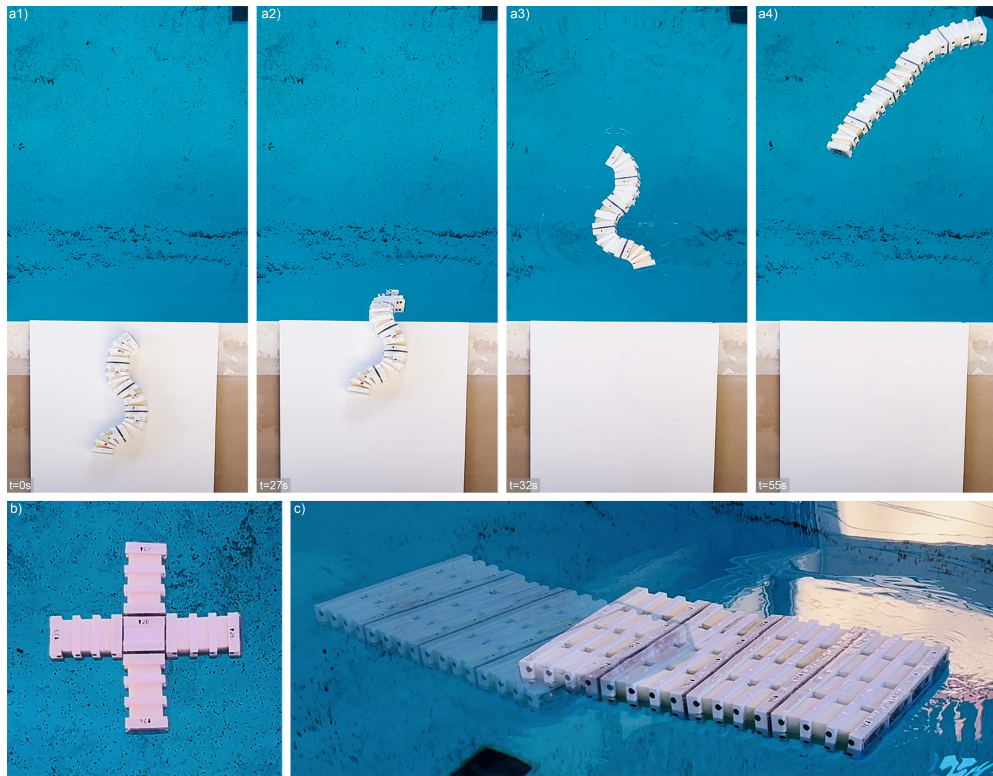
331 Contactless manipulation involves moving objects by generating water currents rather  
332 than through direct physical contact. As shown in Fig. 6(b) and Movie S1, two chains  
333 of robots can form a tunnel to create a directed water current. This controlled flow  
334 transports objects without direct interaction, with each robot contributing to the  
335 stability and consistency of the current. The tunnel method operates similarly to the  
336 concept of a fish ladder, where a controlled current guides objects through the tunnel  
337 with precision and consistency.

### 338 **Locomotion**

339 Our modular robots can achieve diverse locomotion strategies by adopting different  
340 configurations and control approaches tailored to specific environments and tasks. The  
341 arrangement of modules determines the propulsion mechanism and the control strat-  
342 egy required for efficient movement. For example, chain configurations enable both  
343 amphibious locomotion and adaptability in transitioning between ground and water,  
344 while symmetrical arrangements like the plus-sign configuration allow for omnidirec-  
345 tional movement with precise control. Below, we present two examples illustrating how  
346 these configurations are optimized for distinct locomotion tasks.

### 347 **Amphibious locomotion using a chain of modules**

348 Inspired by the undulatory gait of snakes, we developed a gait for ground locomotion  
349 that achieves diagonal forward motion through coordinated and asymmetric lateral  
350 bending, similar to gaits used in other snake robots [30, 31]. In this method, five  
351 modules are connected into a chain, as shown in Fig. 7(a) and Movie S1. The gait  
352 alternates between bending modules 1, 2, and 5 in one direction (e.g., left) and modules  
353 3 and 4 in the opposite direction (e.g., right), creating an unbalanced wave-like motion.  
354 This actuation sequence is then reversed, with modules 1, 2, and 5 bending to the  
355 right and modules 3 and 4 to the left. The asymmetric pattern introduces mechanical  
356 imbalance, which propels the robot diagonally forward, even on surfaces with isotropic



**Fig. 7 Examples of locomotion capabilities.** (a) Amphibious locomotion inspired by the undulation of a snake. The robot demonstrates snake-like movement on the ground (a1–a2) and utilizes a propeller for locomotion in water (a4). (b) Omni-directional locomotion demonstrated using a cross-shaped (+) configuration, enabling movement in all directions. (c) Lattice locomotion is achieved by actuating the propellers of modular units in different patterns, allowing coordinated movement of the entire structure.

357 friction. Due to the placement of the propellers, the modules are inverted during  
 358 ground locomotion, with the propellers positioned on the top side of the chain to avoid  
 359 interference with the ground.

360 When the chain of modules transitions into water, the center of mass causes the  
 361 structure to self-right, flipping over so that the propellers are positioned underneath  
 362 the body. Once in this orientation, the propellers are activated to provide efficient  
 363 locomotion in the water, enabling smooth amphibious movement.

364 This dual locomotion strategy highlights the adaptability of the modular robot  
 365 system, enabling seamless transitions from ground to aquatic environments. The sys-  
 366 tem leverages different mechanisms for propulsion in each domain, with a self-righting  
 367 capability ensuring stability and functionality during the transition from ground to  
 368 water. However, the reverse transition—from water to ground—has not yet been  
 369 demonstrated and remains a potential area for future exploration.

## 370 **Omni-directional locomotion in plus-sign configuration**

371 When five modules are assembled into a plus-sign configuration, the middle module is  
372 compressed to serve as a connector, linking the four surrounding modules, as shown  
373 in Fig. 7(b) and Movie S1 . This configuration enables omnidirectional locomotion,  
374 allowing the robot to move in eight different directions by coordinating the actuation  
375 of the propellers on the modules, following a thruster-vector configuration used  
376 in several classic underwater remotely operated vehicles. For instance, to move the  
377 robot diagonally toward the right-forward direction, the propellers on the left and  
378 back modules should rotate in the positive direction, while the propellers on the front  
379 and right modules should rotate in the negative direction. This coordinated actuation  
380 produces the desired net force to move the robot in the specified direction.

381 The plus-sign configuration demonstrates the versatility of the modular design,  
382 enabling precise control and movement across multiple directions, making it suitable  
383 for tasks requiring high maneuverability in dynamic environments.

## 384 **Discussion**

385 This work demonstrates the versatility and adaptability of aquatic soft modular robots,  
386 highlighting their potential to address complex tasks in aquatic environments. The  
387 proposed design integrates modularity, softness, and amphibious capabilities, enabling  
388 the robots to perform diverse functionalities such as locomotion, manipulation, and  
389 structure formation. The ability to transition between soft and rigid states through the  
390 combination of rigid and soft foam components allows the robots to adapt to a wide  
391 range of tasks, from forming stable structures to performing precise manipulations.

392 The locomotion strategies demonstrated by the modular robots, including the  
393 amphibious undulation gait and the omnidirectional plus-sign configuration, highlight  
394 their ability to operate effectively on both ground and water. In addition, manipula-  
395 tion techniques such as caging, grasping, peristaltic motion, and contactless methods  
396 showcase their versatility in interacting with objects without traditional grasping  
397 mechanisms, providing effective solutions for handling irregularly shaped or fragile  
398 items. Beyond locomotion and manipulation, the robots excel in structure formation,  
399 creating dynamic assemblies like flat lattices for temporary platforms, such as drone  
400 landing pads, or larger lattices for constructing structures like bridges. The ability to  
401 reconfigure into various shapes, including chains, plus-signs, and connected lattices,  
402 emphasizes the adaptability of the modular design, enabling a broad range of tasks  
403 and applications in aquatic environments.

404 While the results highlight the promise of the system, several limitations must be  
405 addressed in future work. The cable-driven actuation system, though lightweight and  
406 precise, relies on robust waterproofing measures, such as shaft seals and PMMA cov-  
407 ers, which may face durability challenges during extended operation. Additionally, the  
408 reliance on propellers for aquatic locomotion introduces constraints in energy efficiency  
409 and speed, suggesting the need for alternative propulsion methods, such as bio-inspired  
410 fin mechanisms, to improve performance. The connection mechanism, using perman-  
411 ent magnets, provides secure and reliable attachment between modules, unaffected  
412 by external forces. However, the current system does not support active detachment

413 between individual modules. Detachment is limited to pre-defined points within a con-  
414 nected chain of modules, which constrains the reconfiguration process. Incorporating  
415 an active connection mechanism could enable more efficient attachment and detach-  
416 ment, allowing for greater flexibility in dynamic tasks. Furthermore, as the complexity  
417 of control increases with larger configurations, more advanced algorithms will be nec-  
418 essary to optimize coordination and performance. Finally, the structural integrity of  
419 modular assemblies, such as lattices and bridges, requires further exploration under  
420 real-world dynamic conditions, particularly for validating load-bearing capabilities.

421 This research establishes a foundation for advancing aquatic soft modular robots  
422 by combining modularity, deformability, and amphibious functionality into a single  
423 system. Enhancements in durability, propulsion, and control, alongside rigorous field  
424 validation, will be crucial for realizing their full potential. These robots hold promise  
425 for applications in environmental monitoring, underwater exploration, and disaster  
426 relief, offering a modular and adaptable solution for aquatic environments.

## 427 **Methods**

### 428 **Block fabrication and design**

429 The fabrication of each SoftRaft module combines simplicity, functionality, and adapt-  
430 ability, utilizing lightweight materials and precise manufacturing techniques. The  
431 specifications of a single SoftRaft robot are provided in Table. 1, where the weight of a  
432 single module is 384 g. The rigid head and tail are 3D-printed using Resin, chosen for  
433 its high precision and waterproof feature. The rigid middle parts are 3D-printed using  
434 PETG. The PMMA covers is laser cut. The soft foam core is 32D in stiffness, weighs  
435 11 g, and is selected for its buoyancy and flexibility, enabling smooth deformation  
436 during transitions between soft and rigid states.

437 The cable-driven system is powered by an N20 DC motor equipped with a mag-  
438 netic encoder (12V, 50,000 rpm, 1:100 gear ratio), providing precise control over string  
439 lengths for deformation and steering. The propeller motor, used for aquatic locomotion,  
440 model FC130BV-13215/42N-R. Each N20 motor weighs 10.9 g, while the whole  
441 propeller structure weighs 25.5 g. N35 magnets, embedded for modular connectiv-  
442 ity, have a thickness of 3 mm and a diameter of 12 mm, ensuring robust and secure  
443 attachment between modules.

444 Waterproofing measures include silicone glue (TIAN MU<sup>®</sup> 702) and waterproof  
445 grease (YIJIALIN<sup>®</sup> RUBBER SILICON) for sealing sensitive components. The total  
446 weight of the battery (27.5 g), PCB (13.2 g), and other electronic components ensures  
447 that each module maintains a lightweight design without compromising functionality.  
448 By distributing components between the head and tail sections, we achieve the robot's  
449 optimal mass-buoyancy equilibrium.

450 The circuit and control flow, as shown in Fig. 8, highlight the modular integration  
451 of electronic components. The ESP32-S2 microcontroller is used for communication  
452 and control. The system is supplied with a 3.7V 903052 1,800 mAh Li-ion battery, con-  
453 verted to three 12V and one 3.3V for operation. The control flow design incorporates  
454 motor drivers, power monitors, and sensors such as a Hall effect sensor encoder for



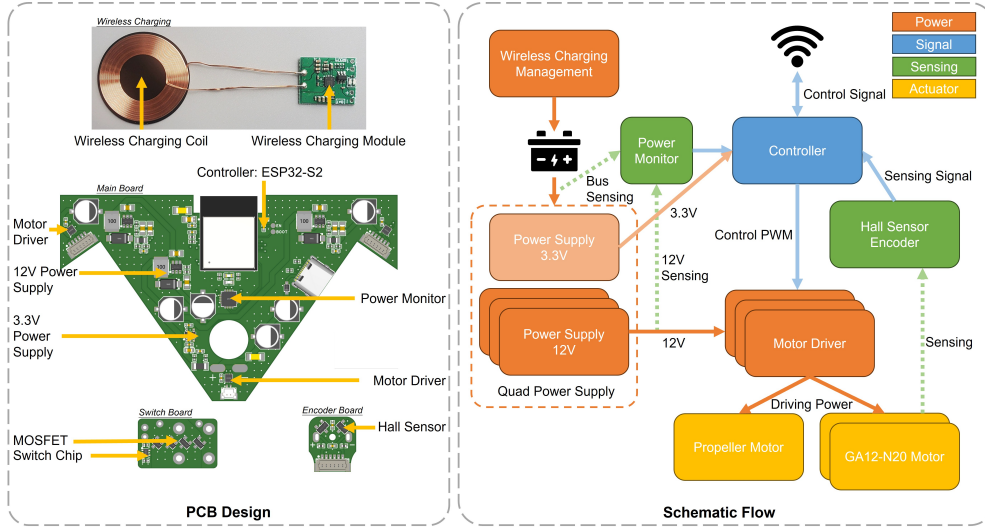


Fig. 8 The design of PCB and circuit control flow.

455 precise actuation feedback. Wireless charging capabilities are integrated using a ded-  
 456 icated coil and charging module, allowing charging without breaking the waterproof  
 457 sealing.

## 458 Experimental design and data analysis

459 To measure the maximum load capacity of a single robot, four modules are connected  
 460 in a 2x2 compressed lattice configuration to ensure stability during the test. A rectan-  
 461 gular container is placed on top of the structure, and sand is gradually added until the  
 462 structure is submerged. This process is repeated across five trials, and the maximum  
 463 load capacity was reported as the average of these experiments.

464 All application experiments were conducted in a swimming pool under uniform  
 465 conditions without additional environmental preparation. Robots were connected to a  
 466 centralized control terminal via Wi-Fi modules. Commands were issued by an operator  
 467 using a laptop connected to the same Wi-Fi network as the robots. The central-  
 468 ized terminal enabled precise control of individual modules and coordinated actions  
 469 across multiple robots. All modules were fabricated identically to ensure consistency  
 470 in experimental results.

471 To analyze and compare the robot's performance across different gaits (Figure S1),  
 472 we collected positional and orientational data using a setup involving an AprilTag  
 473 attached to the top of the robot and a top-mounted camera for tracking. This setup  
 474 enabled precise measurement of the robot's  $x$ ,  $y$ , and  $\theta$  values. For each gait, includ-  
 475 ing forward, backward, left\_front, right\_front, left\_back, and right\_back, we conducted  
 476 35 trials. During these experiments, the robot started from various random initial  
 477 positions and orientations. Using the recorded changes in distance ( $\Delta\text{distance}$ ) and  
 478 orientation ( $\Delta\theta$ ), we transformed the data into a standardized local reference frame,

479 assuming the robot’s initial position and orientation as  $(0, 0, 0)$ , with the orientation  
480 aligned to the  $x$ -axis. To ensure the analysis was robust and focused on typical gait  
481 behaviors, we filtered the data to remove outliers for each gait, retaining 30 data points  
482 that were representative of the robot’s performance. The cleaned data was then ana-  
483 lyzed to determine cluster centers representing the robot’s average behavior for each  
484 gait, and these clusters were visualized to illustrate the motion patterns exhibited by  
485 the robot.

486 The control logic for the experiments and kinematic analyses was implemented in  
487 Python, while configuration space calculations were performed using MATLAB.

## 488 Data availability

489 All data needed to evaluate the conclusions in the paper are present in the paper or  
490 the Supplementary Materials. Computer code is available from the first author and  
491 corresponding authors upon request.

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597 **Competing interests:** The authors declare they have no competing interests.

## 598 Supplementary Materials

599 **This PDF file includes:**

600 Methods

601 Figures S1 to S2

602 Tables S1

603 **Other Supplementary Material for this manuscript includes the following:**

604 Movies S1

## 605 Supplementary Methods

### 606 Kinematics of Modular Robot

607 In this section, we derive the analytical relationships between the string lengths  
608  $s_1$ ,  $s_2$ , the angle  $\theta$ , and the length  $L$  of the middle curve of a robotic structure. The  
609 structure is composed of four rigid 3D-printed components denoted by  $r_1$ ,  $r_2$ ,  $r_3$ ,  
610 and  $r_4$ , each with length  $l_r$ . Figure S2 illustrates the geometric configuration of the  
611 structure.

#### 612 **Forward Kinematics: Given $s_1$ and $s_2$ , find $\theta$ and $L$**

613 The string lengths  $s_1$  (left) and  $s_2$  (right) determine the configuration of the robot.  
614 The components  $\vec{r}_1$ ,  $\vec{r}_2$ ,  $\vec{r}_3$ , and  $\vec{r}_4$  are vectors extending from a common point  $O_1$ ,  
615 and the angle  $\theta$  is the signed angle between  $\vec{r}_1$  and  $\vec{r}_4$ . The vectors  $\vec{r}_2$  and  $\vec{r}_3$  divide  
616 this angle  $\theta$  into three equal parts. The middle curve of the structure is represented  
617 by  $L$ , given by  $L = 3l_2$ , where  $l_2$  is the length of each segment.

618 When  $s_1 \leq s_2$ , we derive the following relationships:

619 Using the triangular similarity principle, the relationship between  $b$ ,  $l_r$ ,  $s_1$ , and  $s_2$   
620 is given by:

$$\frac{b}{b + l_r} = \frac{s_1/3}{s_2/3}, \quad \Rightarrow \quad b = \frac{s_1 \cdot l_r}{s_2 - s_1}.$$

621 To determine the angle  $\theta$ , we apply the cosine rule:

$$\left(\frac{s_1}{3}\right)^2 = b^2 + b^2 - 2b^2 \cos\left(\frac{\theta}{3}\right), \quad \Rightarrow \quad \theta = 3 \cos^{-1}\left(1 - \frac{(s_2 - s_1)^2}{18l_r^2}\right). \quad (1)$$

622 The total length  $L$  of the middle curve can be calculated as:

$$L = \frac{s_1 + s_2}{2}. \quad (2)$$

623 When  $s_1 > s_2$ , the angle  $\theta$  becomes negative, and we adjust the formula  
624 accordingly:

$$\theta = -3 \cos^{-1} \left( 1 - \frac{(s_2 - s_1)^2}{18l_r^2} \right), \quad L = \frac{s_1 + s_2}{2}.$$

625 At the initial state,  $s_1 = s_2 = L$ , and  $\theta = 0$ .

626 **Inverse Kinematics: Given  $\theta$  and  $L$ , find  $s_1$  and  $s_2$**

627 To solve for  $s_1$  and  $s_2$  given the configuration parameters  $L$  and  $\theta$ , we use the  
628 following relationships derived from equations (1) and (2):

629 When  $\theta \geq 0$ , the string lengths  $s_1$  and  $s_2$  are given by:

$$s_1 = L - \frac{1}{2}\Delta s, \quad s_2 = L + \frac{1}{2}\Delta s,$$

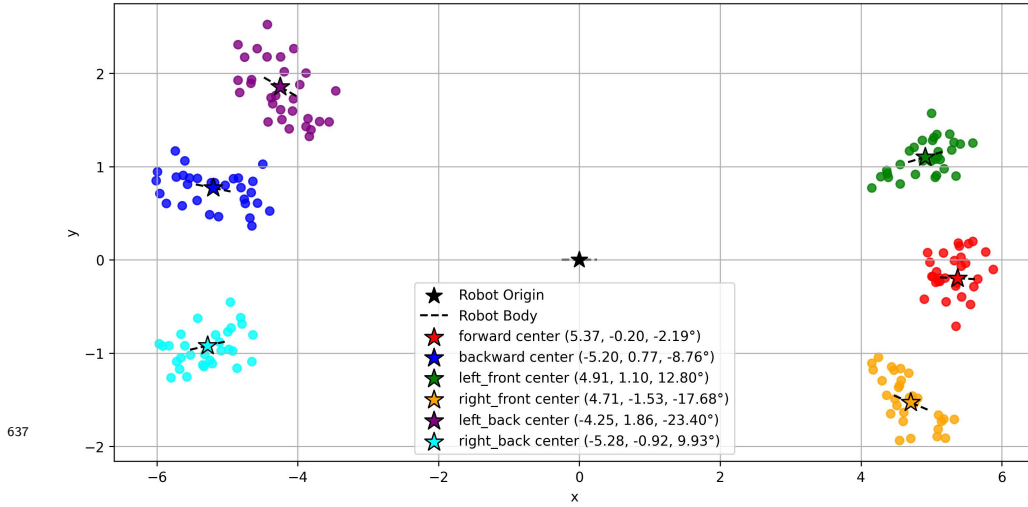
630 where

$$\Delta s = \sqrt{18l_r^2 \left( 1 - \cos \left( \frac{\theta}{3} \right) \right)}.$$

631 If  $\theta < 0$ , swap the values of  $s_1$  and  $s_2$  to reflect the negative angle.

632 We have derived the relationships between the string lengths  $s_1$ ,  $s_2$ , the angle  $\theta$ ,  
633 and the length  $L$  of the middle curve of the structure. These relationships provide  
634 insights for the kinematic analysis and control of the robotic system.

636



637

**Figure S1: Comparison of x-y positions for different gaits and their corresponding cluster centers with positions and orientations.** The figure illustrates the global positions achieved by the robot under six different gaits: forward, backward, left front, right front, left back, and right back. The robot starts at an initial position and orientation of  $(0, 0, 0)$ , with the initial orientation parallel to the x-axis. Cluster centers for each gait are marked with stars (\*), showing their corresponding positions  $(x, y)$  and orientations  $(\theta)$ . Dashed lines at each cluster center indicate the robot's body orientation based on the average  $\theta$  of the gait. The origin  $(0, 0)$  represents the robot's starting position, and the dashed black line at the origin indicates its initial orientation.



638

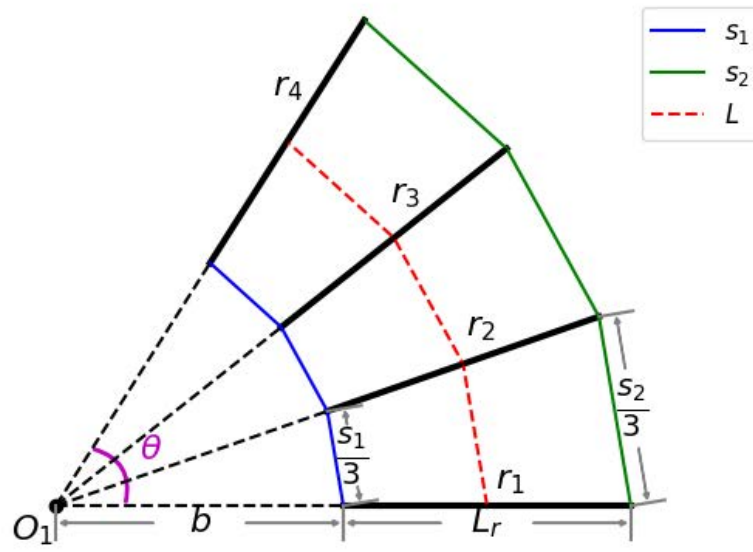


Figure S2: Geometric relationships in the modular robot's kinematics, illustrating the parameters  $s_1$ ,  $s_2$ ,  $\theta$ , and  $L$ . The diagram depicts the four rigid components ( $r_1$ ,  $r_2$ ,  $r_3$ ,  $r_4$ ) extending from a common point  $O_1$ , with angle  $\theta$  divided equally by  $r_2$  and  $r_3$ .

639 **Supplementary Table**

640

**Table 1** Specs of a single SoftRaft Robot.

<b>Parts</b>	<b>Specification</b>	<b>Parameters</b>	<b>Values</b>
Magnet	2.8 g/unit	Dimensions (original)	200×100×118 mm
Battery	903052 1,800 mAh (27.5 g)	Dimensions (compressed)	100×100×118 mm
SoftRaft rigid components	200.3 g	CoT	68.35
Foam	80×145×60 mm 32D (11 g)	Max swimming speed	0.33 m/s
Motor (cable-driven)	GA-N20 (10.9 g/unit)		
Motor (propeller)	FC130-13215/42N (25.5 g)		
PCB and wires	see Fig. 8 (21.2 g)		
Net weight	384 g		